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# Predictable Rain ?

Steganalysis of Public-Key Steganography using Wet Paper Codes

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# Outline

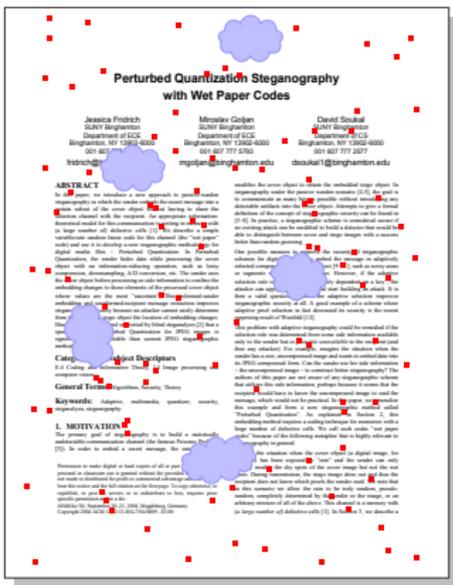
1. Related Work
2. Estimating Embedding Positions
3. Weighted Stego-Image Steganalysis
4. Empirical Results
5. Discussion & Conclusion



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# Wet Paper Codes (WPC)



- ▶ paper exposed to rain
  - ▶ **dry:** possible embedding position
  - ▶ **wet:** excluded
- ▶ dries out during transmission
- ▶ embedding positions unknown to recipient
- ▶ WPC enable extraction of message

Fridrich, Goljan and Soukal (2004)

## Wet Paper Codes (WPC)

- ▶ recipient

$$\begin{array}{c} \boxed{\mathbf{D}} \\ \text{shared matrix} \end{array} \times \begin{array}{c} \boxed{\mathbf{b}} \end{array} = \begin{array}{c} \boxed{\mathbf{m}} \end{array}$$

- ▶ sender solves for change vector  $\mathbf{v}$

$$\begin{array}{c} | \mathbf{m} | \\ \left\{ \begin{array}{c} \overbrace{\boxed{\mathbf{D}}}^n \\ \end{array} \right\} \times \begin{array}{c} \boxed{0} \\ V_2 \\ \vdots \\ \boxed{0} \\ V_n \end{array} = \begin{array}{c} \boxed{\mathbf{m}} \end{array} - \boxed{\mathbf{D}} \times \begin{array}{c} \boxed{b_1} \\ b_2 \\ \vdots \\ \boxed{b_{n-1}} \\ b_n \end{array}
 \end{array}$$

Fridrich et al. (2005a)

## Wet Paper Codes (WPC)

- ▶ recipient

$$\begin{array}{c} \boxed{\mathbf{D}} \\ \text{shared matrix} \end{array} \times \begin{array}{c} \boxed{\mathbf{b}} \end{array} = \begin{array}{c} \boxed{\mathbf{m}} \end{array}$$

- ▶ sender solves for change vector  $\mathbf{v}$

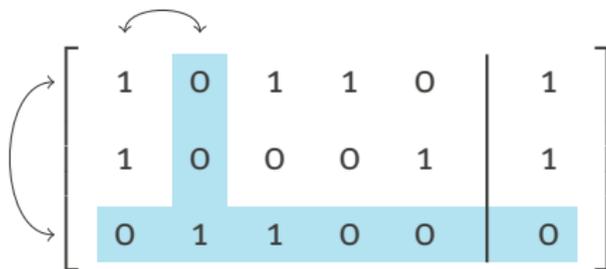
$$|\mathbf{m}| \left\{ \begin{array}{c} \overbrace{\boxed{\mathbf{H}}}^k \\ \boxed{\mathbf{H}} \end{array} \right\} \times \begin{array}{c} \boxed{\mathbf{v}} \end{array} = \begin{array}{c} \boxed{\mathbf{m}} \end{array} - \begin{array}{c} \boxed{\mathbf{D}} \end{array} \times \begin{array}{c} \boxed{\mathbf{b}} \end{array}$$

Fridrich et al. (2005a)

## Matrix LT Process

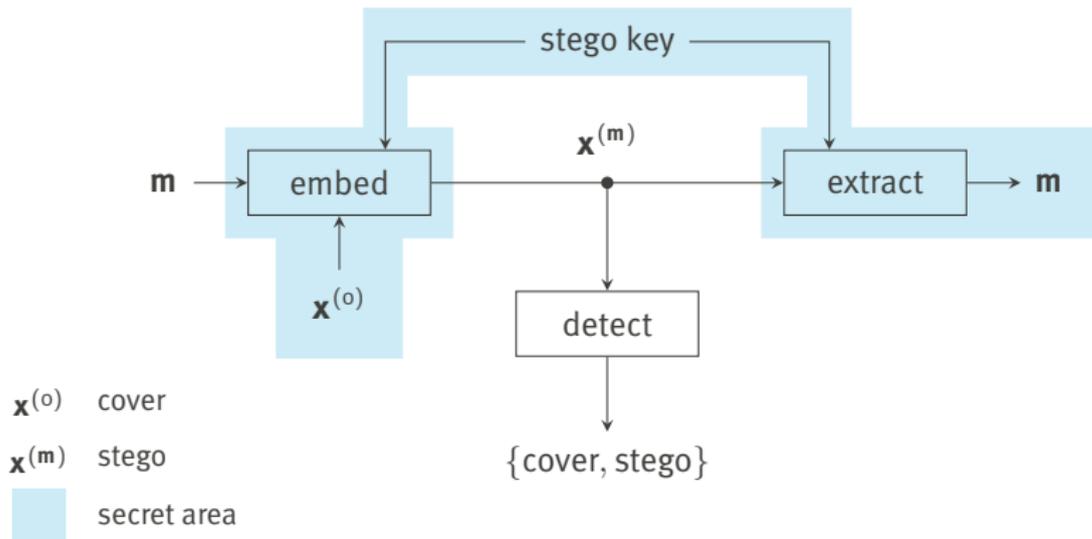
- ▶ upper triangle form by permuting rows and columns
- ▶ generate Matrix **D** following Robust Soliton Distribution (RSD)

Luby (2002)

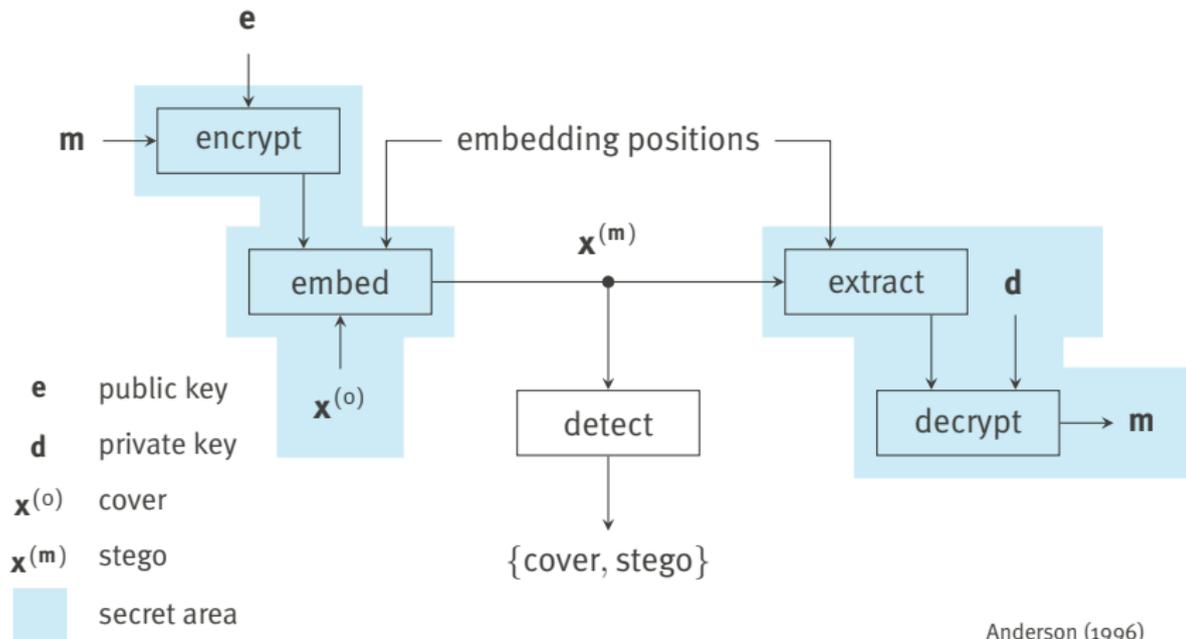

$$\left[ \begin{array}{ccccc|c} 1 & 0 & 1 & 1 & 0 & 1 \\ 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 0 \end{array} \right]$$

Fridrich et al. (2005b)

# Steganography

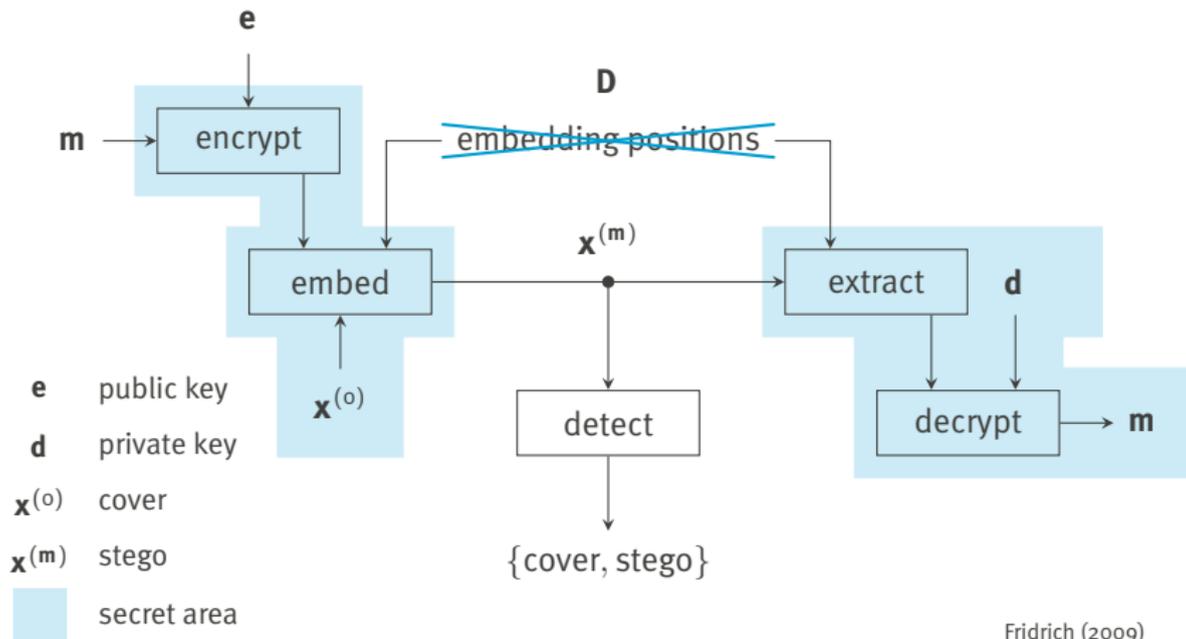


# Public-Key Steganography (PKS)



Anderson (1996)

# Public-Key Steganography (PKS)



Fridrich (2009)

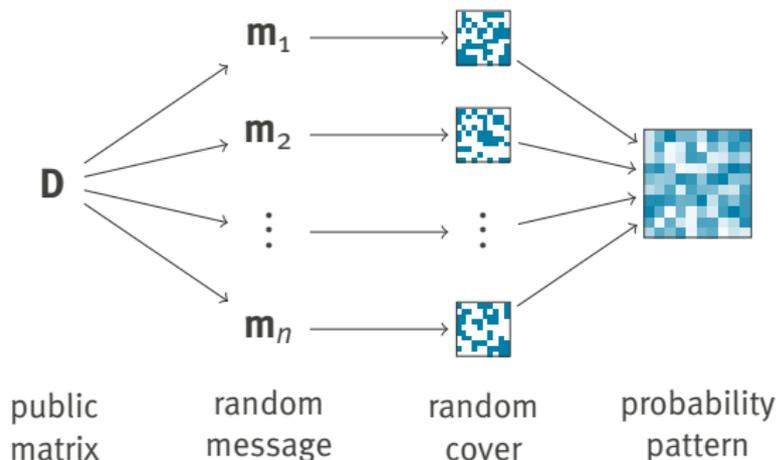


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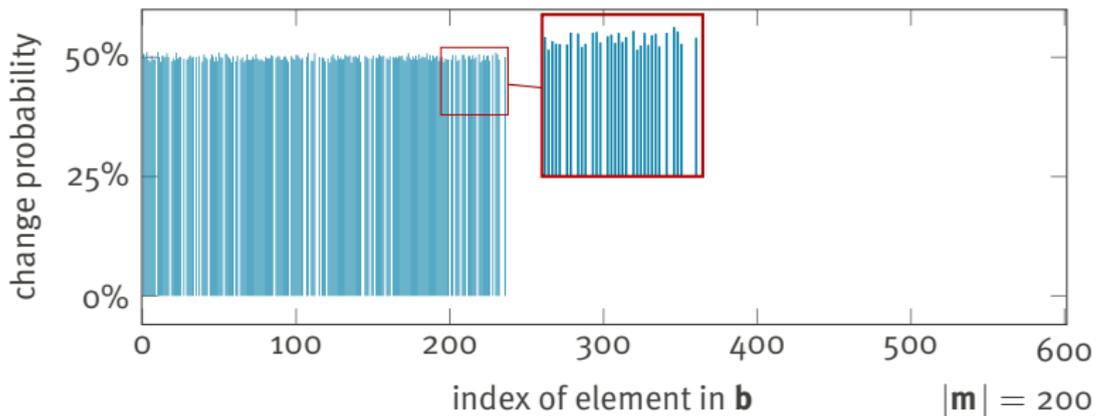
## Estimating Embedding Positions

- ▶ matrix LT process favours certain columns
- ▶ large part of system of linear equations is public due to **D**
- ▶ calculate probability patterns based on **D**



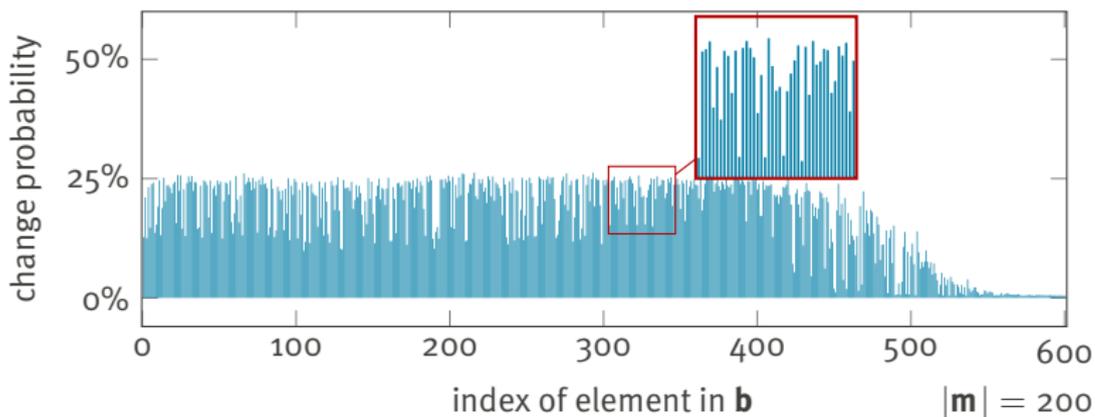
## Probability Pattern

- ▶ matrix LT process
- ▶ no 'wet' pixels



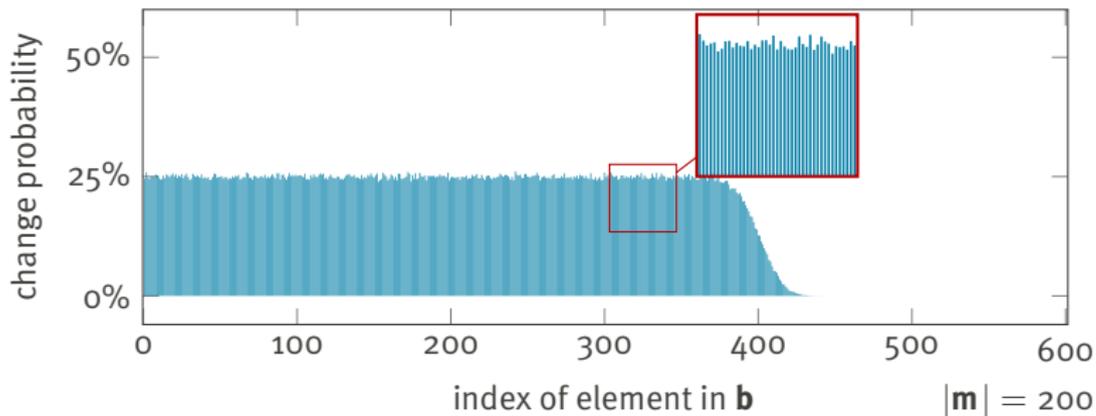
## Probability Pattern

- ▶ matrix LT process
- ▶ 50% 'wet' pixels



## Probability Pattern

- ▶ Gaussian elimination
- ▶ 50% 'wet' pixels

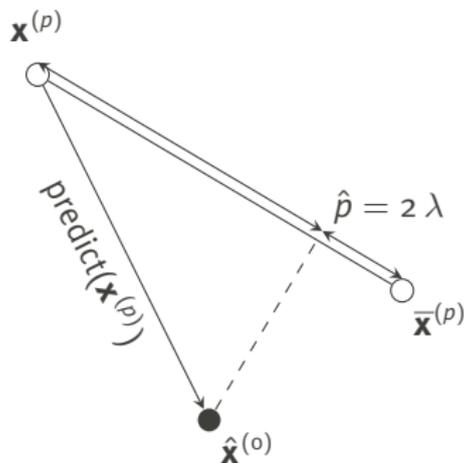




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## Weighted Stego-Image (WS) Steganalysis



- $\mathbf{x}^{(o)}$  cover
- $\hat{\mathbf{x}}^{(o)}$  estimated cover
- $\mathbf{x}^{(p)}$  stego
- $\bar{\mathbf{x}}^{(p)}$  stego, all LSBs flipped
- $p$  payload
- $\lambda$  weighting

Weighted Stego-Image (WS):

$$\mathbf{x}^{(p,\lambda)} = \lambda \bar{\mathbf{x}}^{(p)} + (1 - \lambda) \mathbf{x}^{(p)}$$

Estimator of embedding rate:

$$\hat{p} = 2 \arg \min_{\lambda} \sum_{i=1}^n \left( x_i^{(p,\lambda)} - \hat{x}_i^{(o)} \right)^2$$

Theorem 1 of Fridrich and Goljan (2004)

## Adding Predictability Weights

|          |          |             |          |          |
|----------|----------|-------------|----------|----------|
| $x_1$    | $x_2$    | $x_3$       | $x_4$    | $x_5$    |
| $x_6$    | $x_7$    | $\hat{x}_8$ | $x_9$    | $x_{10}$ |
| $x_{11}$ | $x_{12}$ | $x_{13}$    | $x_{14}$ | $x_{15}$ |
| $x_{16}$ | $x_{17}$ | $x_{18}$    | $x_{19}$ | $x_{20}$ |
| $x_{21}$ | $x_{22}$ | $x_{23}$    | $x_{24}$ | $x_{25}$ |

Weighted WS Steganalysis

$$\hat{p} = 2 \arg \min_{\lambda} \sum_{i=1}^n w_i \left( x_i^{(p, \lambda)} - \hat{x}_i^{(0)} \right)^2$$

- ▶ weighting takes predictability into account

Theorem 3 of Fridrich and Goljan (2004)

## Adding Predictability Weights

|          |          |          |          |          |
|----------|----------|----------|----------|----------|
| $x_1$    | $x_2$    | $x_3$    | $x_4$    | $x_5$    |
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### Probability WS Steganalysis

$$\hat{p} = 2 \arg \min_{\lambda} \sum_{i=1}^n \omega_i \left( x_i^{(p,\lambda)} - \hat{x}_i^{(0)} \right)^2$$

- ▶ weighting takes predictability into account
- ▶ replace weight with normalized probabilities:

$$\omega_i = \frac{p_i}{\sum_{j=1}^n p_j}$$

Theorem 3 of Fridrich and Goljan (2004)

## Sorting the Stego-Image

|          |          |          |          |          |
|----------|----------|----------|----------|----------|
| $p_2$    | $p_{25}$ | $p_1$    | $p_4$    | $p_{22}$ |
| $p_7$    | $p_8$    | $p_{17}$ | $p_{14}$ | $p_{15}$ |
| $p_{18}$ | $p_5$    | $p_{16}$ | $p_{11}$ | $p_{24}$ |
| $p_{10}$ | $p_9$    | $p_{13}$ | $p_{21}$ | $p_{19}$ |
| $p_3$    | $p_6$    | $p_{12}$ | $p_{23}$ | $p_{20}$ |

### Sequential WS Steganalysis

$$E(l) = \sum_{i=1}^l \left( \frac{1}{2} \left( x_i^{(p)} + \bar{x}_i^{(p)} \right) - \hat{x}_i^{(0)} \right)^2 + \sum_{i=l+1}^n \left( x_i^{(p)} - \hat{x}_i^{(0)} \right)^2$$

- ▶ assumes initial sequential embedding

Ker (2007)

## Sorting the Stego-Image

|          |          |          |          |          |
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- ▶ assumes initial sequential embedding
- ▶ reorder stego-image according to probabilities

Ker (2007)

## Sorting the Stego-Image

|          |          |          |          |          |
|----------|----------|----------|----------|----------|
| $y_1$    | $y_2$    | $y_3$    | $y_4$    | $y_5$    |
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### Sorted WS Steganalysis

$$E(l) = \sum_{i=1}^l \left( \frac{1}{2} \left( y_i^{(p)} + \bar{y}_i^{(p)} \right) - \hat{y}_i^{(o)} \right)^2 + \sum_{i=l+1}^n \left( y_i^{(p)} - \hat{y}_i^{(o)} \right)^2$$

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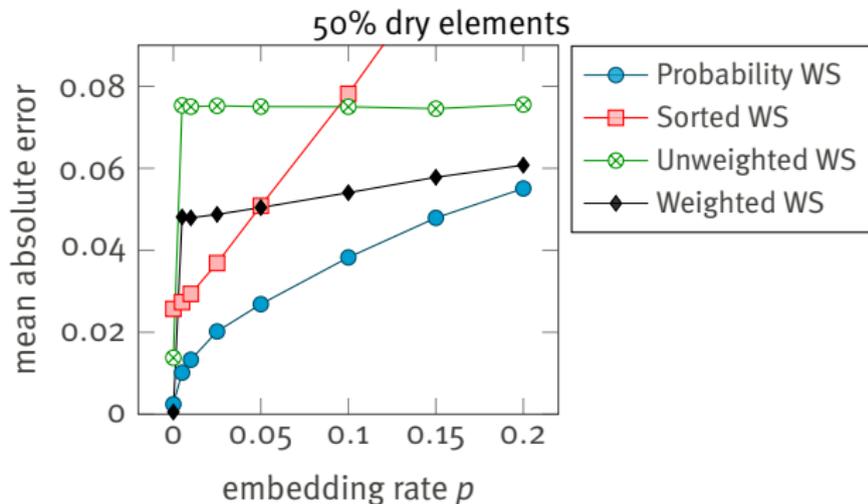
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## Empirical Results

- ▶ 10,000 BOSSBase images, cropped to  $128 \times 128$  pixels
- ▶ amount of dry elements unknown

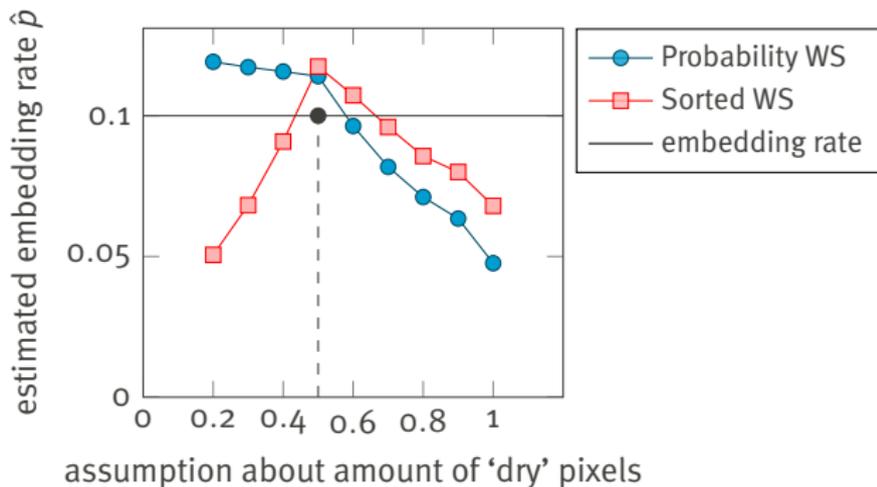
Bas et al. (2011)



## Empirical Results

- ▶ 10,000 BOSSBase images, cropped to  $128 \times 128$  pixels
- ▶ amount of dry elements unknown
- ▶ estimate by using the point where both methods yield a similar result

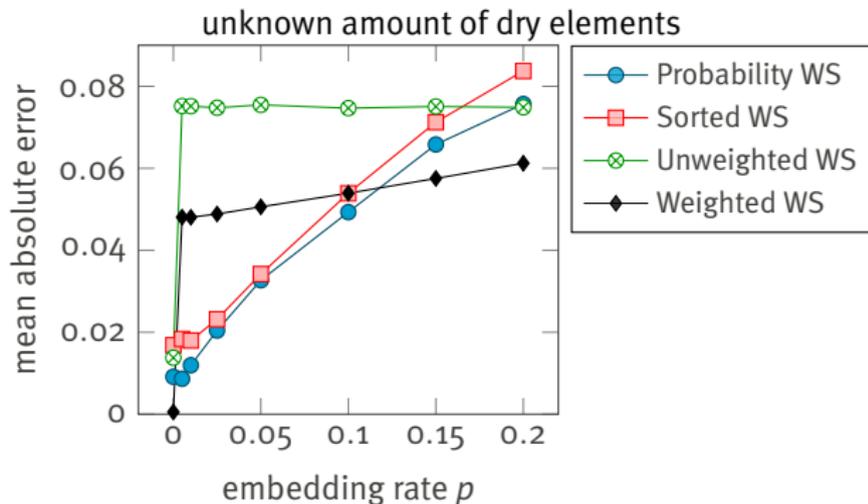
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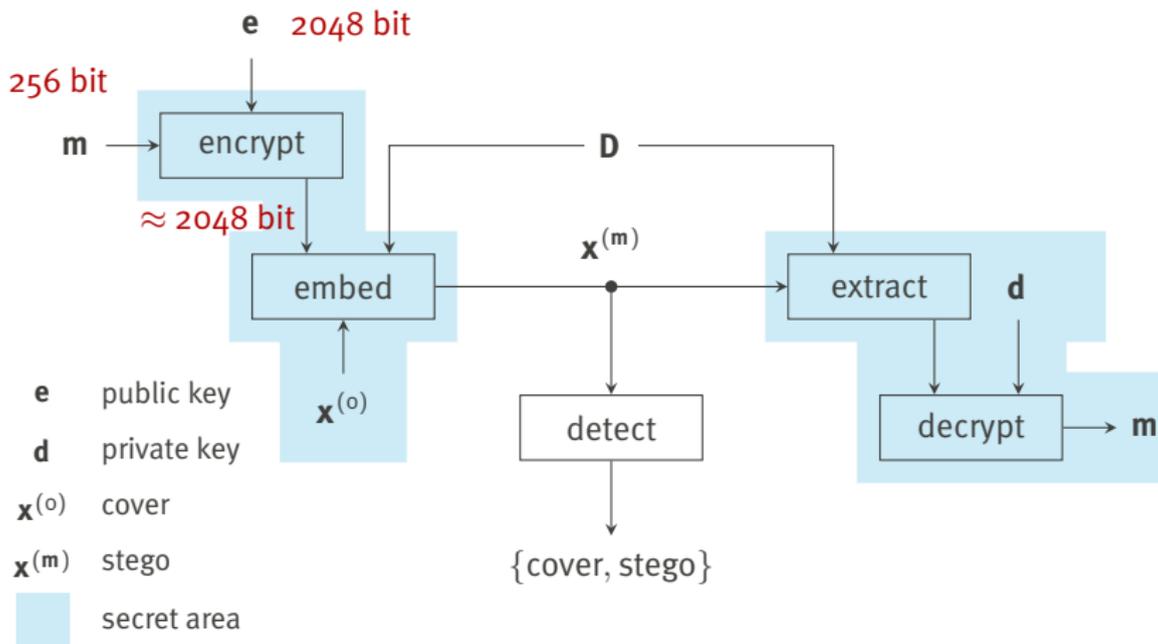




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# Relevance



## Conclusion

- ▶ WPC enable secret embedding positions in PKS
- ▶ public matrix allows calculation of probability patterns
- ▶ probability patterns independent of used embedding method
- ▶ extend existing attacks to make them applicable
  - ▶ shown for LSB-Replacement
  - ▶ two extensions of WS steganalysis
- ▶ also relevant in a key encapsulation scheme
- ▶ Predictable Rain?



## Conclusion

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- ▶ public matrix allows calculation of probability patterns
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- ▶ extend existing attacks to make them applicable
  - ▶ shown for LSB-Replacement
  - ▶ two extensions of WS steganalysis
- ▶ also relevant in a key encapsulation scheme
- ▶ Predictable Rain?
  - ▶ predict the most likely *hideouts in the storm*

Questions?



## References I

- Anderson, Ross J. (1996). ‘Stretching the limits of steganography’. In: *Information Hiding (1st International Workshop)*. Ed. by Ross J. Anderson. Vol. 1174. Lecture Notes in Computer Science. Berlin Heidelberg: Springer-Verlag, pp. 39–48.
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- Fridrich, Jessica, Miroslav Goljan, Petr Losiněk and David Soukal (2005a). ‘Writing on wet paper’. In: *IEEE Transactions on Signal Processing* 53.10, pp. 3923–3935.

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